

THE HONG KONG POLYTECHNIC UNIVERSITY

Department of Applied Mathematics

Lightboard Project

7. Limits By L'Hopital's Rule

Evaluate the following limits.

$$7.1 \quad \lim_{x \rightarrow -2} \frac{\cos(x^2 - 4)}{x^2 + x - 6} \quad [21221 \text{ Test2}]$$

$$7.2 \quad \lim_{x \rightarrow 0^+} \frac{x^2 \sin \frac{1}{x}}{e^x - 1}$$

$$7.3 \quad \lim_{x \rightarrow 0^+} e^x (\tan x) \ln(x^2) \quad [21221 \text{ Test2}]$$

$$7.4 \quad \lim_{x \rightarrow \infty} 2^{-x} \ln(x^3 + 2x + 1) \quad [22231 \text{ Exam}]$$

$$7.5 \quad \lim_{x \rightarrow 0} \left(\frac{1}{x^2} - \frac{\sin x}{x^3} \right) \quad [21221 \text{ Test2}]$$

$$7.6 \quad \lim_{x \rightarrow \infty} (\sqrt{x + \ln x} - \sqrt{x})$$

$$7.7 \quad \lim_{x \rightarrow \infty} x^{(e^{-x})} \quad [20211 \text{ Test2}]$$

$$7.8 \quad \lim_{x \rightarrow 0^+} \left(\frac{\sin x}{x} \right)^{\frac{1}{x}} \quad [18192 \text{ Test2}]$$

$$7.9 \quad \lim_{x \rightarrow 0^+} x^{(1 - \cos x)} \quad [\text{Modified from 22231 Test2}]$$

$$7.10 \quad \lim_{x \rightarrow \infty} \left(\frac{1}{x} + 1 \right)^{x^2} e^{-x}$$